1	<b>Moist Static Energy Budget of MJO-like</b>
2	disturbances in the atmosphere of a zonally
3	symmetric aquaplanet
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#### 2

## Abstract

3	A Madden-Julian Oscillation (MJO)-like spectral feature is observed in the time-space
4	spectra of precipitation and column integrated Moist Static Energy (MSE) for a zonally
5	symmetric aquaplanet simulated with Super-Parameterized Community Atmospheric
6	Model (SP-CAM). This disturbance possesses the basic structural and propagation
7	features of the observed MJO.
8	To explore the processes involved in propagation and maintenance of this disturbance,
9	we analyze the MSE budget of the disturbance. We observe that the disturbances
10	propagate both eastwards and polewards. The column integrated long-wave heating is the
11	only significant source of column integrated MSE acting to maintain the MJO-like
12	anomaly balanced against the combination of column integrated horizontal and vertical
13	advection of MSE and Latent Heat Flux. Eastward propagation of the MJO-like
14	disturbance is associated with MSE generated by both column integrated horizontal and
15	vertical advection of MSE, with the column long-wave heating generating MSE that
16	retards the propagation.

17 The contribution to the eastward propagation by the column integrated horizontal 18 advection of MSE is dominated by synoptic eddies. Further decomposition indicates that 19 the advection contribution to the eastward propagation is dominated by meridional 20 advection of MSE by anomalous synoptic eddies caused by the suppression of eddy 21 activity ahead of the MJO convection. This suppression is linked to the barotropic 22 conversion mechanism; with the gradients of the low frequency wind experienced by the 23 synoptic eddies within the MJO envelope acting to modulate the Eddy Kinetic Energy.

- 1 The meridional eddy advection's contribution to poleward propagation is dominated by
- 2 the mean state's (meridionally varying) eddy activity acting on the anomalous MSE
- 3 gradients associated with the MJO.

# 1 1. Introduction

2	In observations of satellite records of equatorial Outgoing Longwave Radiation (OLR,
3	e.g. Liebmann and Smith 1996), there are patterns of enhanced convection and
4	precipitation organized on planetary scales. The strongest and largest of these convective
5	structures propagate eastwards at about 5 m/s with periods in the range of 30 to 90 days
6	from the Indian Ocean to the central Pacific, coupled to planetary scale wind,
7	temperature, and moisture anomalies. This disturbance is known as the Madden-Julian
8	Oscillation (MJO), originally identified in tropical zonal wind soundings by Madden and
9	Julian (1971, 1972). The MJO dynamics involve planetary scale circulations interacting
10	with mesoscale convective systems and potentially the ocean, making it a challenging
11	phenomenon to understand (e.g. Zhang 2005).
12	Understanding the MJO phenomena is important to our grasp of the tropical atmosphere
13	and climate for many reasons. MJO related variations dominate the intraseasonal
14	variability of the tropical ocean-atmosphere system, linking the variabilities of climate
15	and weather (e.g. Lau and Wu 2010). For example, the MJO is seen to influence the
16	rainfall over virtually all regions of the tropics and the subtropics: the Asian Monsoon
17	(e.g. Lau and Chan 1986, Sui and Lau 1992, Lawrence and Webster 2002); the Australian
18	Monsoon (e.g. Hendon and Liebmann 1990); over the Indonesian archipelagos (Hidayat
19	and Kizu 2010); along the west coast of North America (Mo and Higgins 1998, Jones
20	2000, Bond and Vecchi 2003); in South America (Paegle et al. 2000, Liebmann et al
21	2004); and in Africa (Matthews 2004).

22 The MJO has also been observed to modulate the genesis of tropical cyclones in the

1	Pacific and Caribbean basins (e.g. Liebmann <i>et al.</i> 1994, Nieto Ferrira <i>et al.</i> 1996,
2	Maloney and Hartmann 2000, Hall et al, 2001, Higgins and Shi 2001, Frank and Roundy
3	2006). It has been observed that improved forecasts of MJO dynamics may help improve
4	short term Tropical Cyclone forecasting (e.g. Leroy and Wheeler 2008). The MJO affects
5	the global medium and long range weather forecasts (e.g. Ferranti et al. 1990, Hendon et
6	al. 2000, Jones and Schemm 2000); modulates the global angular momentum and the
7	length of the day (e.g. Langley et al. 1981, Gutzler and Ponte 1990, Weickmann et al.
8	1997); and modulates the Earth's electric and magnetic fields, with influence upon
9	lightning activity (e.g. Anyamba et al. 2000).
10	MJO events are usually observed in the Indian and Western Pacific Oceans as large-scale,
11	eastward propagating regions of strong, deep convection and precipitation separating
12	regions of weak convection. The structure usually has a zonal wavenumber of 1 or 2,
13	with a single active region existing at a time. An overturning zonal circulation that
14	extends vertically through the entire troposphere connects the active and inactive phases.
15	The circulation creates zonally converging winds in the boundary layer and lower
16	troposphere (up to about 850 hPa) and zonally diverging winds at about 200 hPa (e.g.
17	Madden and Julian 1972 and Zhang 2005). The coupled wind-convection system
18	propagates at around 5 m/s. The MJO events can be clearly seen in Hovmöller plots of
19	many observed quantities, such as equatorial zonal wind (e.g., Xie and Arkin 1997), or as
20	a very strong peak in wavenumber-frequency spectra of tropical variables such as OLR
21	(e.g. Wheeler and Kiladis 1999).

The description of the MJO as a purely eastward moving monolith of convection is notthe whole picture. For example, the MJO convective region is a multiscale structure,

1	consisting of an ensemble of convective systems moving at many different speeds in all
2	directions (e.g. Nakazawa 1988). The convection in these mesoscale and smaller systems
3	is enhanced by the large-scale conditions in the MJO active region and the motion of the
4	active region is reflected in a general eastward trend in the locations these systems
5	develop and then decay. Another important fact to consider is that the MJO propagation
6	is not always strictly eastwards - meridional motion, generally into the summer
7	hemisphere, is observed over the east Pacific and over southern Asia in some seasons
8	(Typically Boreal Summer; Wang and Rui 1990a).
9	The MJO is one of the dominant structures in the tropical atmosphere and has been
10	observed for almost four decades, so its structure has been quite well determined (e.g.
11	Hendon and Salby 1994, Lau and Sui 1997, Yanai et al. 2000, Kikuchi and Takayabu
12	2004, Kiladis et al. 2005, Haertel et al. 2008), although a sufficiently accurate energy
13	budget remains elusive. At the same time, the theoretical understanding of the
14	mechanisms responsible for its growth and propagation has not kept pace (e.g., Zhang
15	2005, Waliser et al. 2006). Because the convectively coupled Kelvin Waves (KW) have
16	many basic features in common with the MJO (propagation direction, scale, wind field
17	structure), and because theories of the equatorial waves have shown some successes (e.g.
18	Matsuno 1966, Wang 1988, Majda and Shefter 2001, Andersen and Kuang 2008, Kiladis
19	et al. 2009), the KW and the other equatorially trapped shallow water waves are
20	commonly used as a fundamental part of MJO theories. <sup>2</sup>

<sup>2</sup> The equatorially trapped shallow water waves arise from an analysis of the anomalies in temperature and wind of zonally symmetric atmosphere linearized about a stationary

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1 However, the KW propagates much faster than the MJO and is quite distinct from the 2 MJO in spectral space. This leads to the question - in what ways does the convectively coupled KW differ from the MJO? For either of these wave types to exist in observations, 3 4 some process or processes must supply energy (or an analogous quantity) to overcome 5 dissipation selectively at the timescales, wavelengths and velocities of the disturbances. 6 Most theories of the KW assume that the source of the energy for the wave comes from 7 an interaction between convective heating and the large-scale temperature structure of the 8 wave, with scale selection due to the varying sign of the heating/warm anomaly overlap. 9 Such theories have had success replicating the nature of the KW (and other "rotating 10 shallow water" modes) in simple models (e.g. Mapes 2000, Khouider and Majda 2006, 11 Kuang 2008, Andersen and Kuang 2008). Any theory of the MJO requires column Moist 12 Static Energy (MSE) variance to be generated at intraseasonal and planetary scales, with 13 slow eastward propagation. There are a number of potential sources of column MSE 14 variability that are often considered:

mean state. Under the assumptions of constant stratification and a rigid upper boundary on the troposphere, the vertical structure equations can be separated from the horizontal dynamics, which are identical to the equations for shallow water modes, with the separation constant identified as the equivalent depth. Due to the rotation of the earth, the shallow water system has a number of specific modes propagating along the equator, as determined by Matsuno (1969). The convectively coupled shallow water waves tend to exist and propagate because of the interactions between convective heating and the temperature anomalies of the waves.

1	1) An independently existing forcing such as a standing oscillation in the convection
2	over the warm pool, with MJO propagation as a passive atmospheric response (e.g.
3	Zhang and Hendon 1997);
4	2) The column MSE variability is generated by the coupling of convection and
5	circulation. An example of this sort of mechanism is Wave-CISK (e.g. Lau and
6	Peng 1987), where convection releases latent heat that drives further convection by
7	creating more low-level convergence;
8	3) Wind Induced Surface Heat Exchange (WISHE; Emanuel 1987, Neelin et al.
9	1987), where surface wind anomalies lead to surface flux anomalies that may
10	provide an energy source to the convection;
11	4) Instability arising from frictional moisture convergence feedback (e.g. Wang
12	1988);
13	5) Thermodynamic feedbacks - such as water vapor accumulation (Blade and
14	Hartmann 1993) and convection-radiation feedback (Hu and Randall 1994, 1995,
15	Raymond 2001).
16	
17	It is in this last paradigm that we will be interpreting our observations, so it bears further
18	exposition. The Recharge-Discharge mechanism, an extension of the thermodynamic
19	feedback idea, is based upon the build up of MSE in the columns over the tropical ocean

- 20 that occurs before the MJO deep convection. This convection and the succeeding
- 21 processes discharge the column MSE anomaly, which is then recharged by the large-scale

processes (e.g. Hendon and Liebmann 1990, Blade and Hartmann 1993, Hu and Randall
1994, Maloney and Hartmann 1998, Kemball-Cook and Weare 2001, Myers and Waliser
2003, Sobel and Gildor 2003, Kiladis *et al.* 2005, Agudelo *et al.* 2006, Tian *et al.* 2006,
Benedict and Randall 2007, Maloney 2009). In order for Recharge-Discharge to
constitute an instability mechanism, there must be sources of column MSE collocated in
space and time with positive column MSE anomalies (similarly for sinks and negative
MSE anomalies).

8 Recent studies appear to indicate that the moistening of the free troposphere (leading to a 9 build up of MSE) is needed before the onset of strong deep convection (e.g. Brown and 10 Zhang 1997, Sherwood 1999, Raymond 2000, Redelsperger et al. 2002, Ridout 2002, 11 Bretherton et al. 2004, Derbyshire et al. 2004, Sobel et al. 2004, Takemi et al. 2004, 12 Roca et al. 2005, Kuang and Bretherton 2006, Peters and Neelin 2006). Similarly, 13 parameterizations that demonstrate a strong sensitivity to free-troposphere humidity have 14 been shown to increase intraseasonal variability in GCMs (e.g. Wang and Schlesinger 15 1999, Woolnough et al. 2001). Ocean heat content may also be built up before the onset 16 of convection, with the surplus heat flowing into the atmosphere during the convective 17 phase (e.g. Sobel and Gildor 2003, Stephens et al. 2004, Agudelo et al. 2006). In general, 18 the MSE budget during MJO events is not well understood, although there have been 19 recent numerical studies of this question (Maloney 2009, Maloney et al. 2010). 20 In another recent study of the MSE budget of large-scale tropical flows (Kuang 2011), it 21 has been shown that the large-scale flow induced by MSE anomalies in a column, while 22 acting to dissipate the column MSE anomaly, will become less efficient at doing so with 23 longer wavelengths. This is because the temperature anomalies required to generate the

large-scale flow increases with wavelength, affecting the vertical distribution of
 convection. This is suggested as a possible scale selection mechanism explaining the
 limitation of the MSE driven waves to long wavelengths.

In analogy to the buoyancy driven KW theories, we will interpret the MJO growth and
propagation as the overlap between "moist" air and "moistening". In this context and
throughout this paper, "moist" is synonymous with a positive MSE anomaly and
"moistening" with an MSE source.

8 The basic picture of the MSE budget in the MJO established to date is as follows: The 9 shallow convection and circulations ahead of the convective anomaly have a moistening 10 tendency, contributing to the MSE build up before the deep convection (e.g. Johnson et 11 al. 1999, Kikuchi and Takayuba 2004, Kiladis et al. 2005, Benedict and Randall 2007). 12 Column-integrated MSE may then be discharged during strong convective and stratiform 13 heating. The large-scale circulations in the Western Pacific and Indian Ocean are strongly 14 determined by the deep convection and have been observed to export MSE for the 15 convecting columns on average (e.g. Neelin and Held 1987, Back and Brethton 2006). In 16 this region the MJO amplitude is strongest and the MSE discharge appears to be 17 enhanced by the MJO deep convective and stratiform stages (e.g. Johnson et al. 1999, 18 Kiladis et al 2005). 19 MSE discharge during MJO convection may be modified by cloud-radiation and wind-

20 evaporation feedbacks, which could reduce or change the sign of the MSE tendency (e.g.

21 Raymond 2001, Lin and Mapes 2004, Peters and Bretherton 2006, Sugiyama 2009a,

22 2009b). Intraseasonal wind speed and latent heat flux anomalies are observed to have a

1 positive covariance with the intraseasonal precipitation (e.g. Zhang 1996, Raymond et al. 2 2003, Masunaga et al. 2006, Maloney and Esbensen 2007, Araligidad and Maloney 3 2008) and wind-evaporation feedbacks have been found to be important for supporting 4 the intraseasonal convection in modeling studies (e.g. Raymond 2001, Maloney and 5 Sobel 2004, Fuchs and Raymond 2005, Sugiyama 2009a, 2009b). However, the WISHE 6 feedbacks are not generally in the original sense of WISHE, where easterly anomalies 7 interact with mean state easterlies to create enhanced flux under the warm anomaly 8 region in KW-type circulation, pulling convection forwards in space (e.g. Emanuel 1987, 9 Neelin et al 1987, Emanuel et al. 1994) to create overlap between the convective heating 10 and the warm anomaly. The intraseasonal latent heat flux-precipitation relationships are 11 consistent with the more general role of enhanced wind speed in supporting tropical 12 precipitation – particularly in regions of high column relative humidity (e.g. Back and 13 Bretherton 2005). Observations also suggest that horizontal advection of temperature and 14 moisture from the cooler, drier subtropics is an important regulatory mechanism for the 15 atmospheric MSE budget and MJO deep convection (e.g. Mapes and Zuidema 1996, 16 Myers and Waliser 2003, Back and Bretherton 2006).

Model analysis of the MSE budget in CAM3 with a realistic basic state shows that
horizontal advection plays an important role in regulating the discharge-recharge cycle.
The advection effect is dominated by the tropical synoptic scale eddies (Maloney 2009).
Maloney (2009) observed a buildup of column MSE in advance of intraseasonal
precipitation within low-level easterly anomalies and a discharge of MSE during and
after the precipitation, within low-level westerlies. The recharge-discharge budget of the
MSE is driven by horizontal advection (somewhat opposed by a mostly out of phase

1	latent heat flux), which is itself dominated by the meridional advection of dry subtropical
2	air into the MJO region by atmospheric eddies, which are suppressed by the anomalous
3	large-scale winds ahead of the convection and enhanced behind.
4	While the eastward propagating MJO dominates the tropical intraseasonal variability, it is
5	not the only significant source of variability on these timescales. For example, there are
6	prominent northward propagating oscillations during the Asian monsoon (Yasunari 1979,
7	Lau and Chan 1986, Wang and Rui 1990a). It has been observed that the MJO eastward
8	propagation weakens during boreal summer (Madden 1986, Wang and Rui 1990a) and a
9	northward propagating feature in the intraseasonal fequencies becomes prominent over
10	the Indian summer monsoon region (e.g. Yasanuri 1979, Sikka and Gadgil 1980,
11	Krishnamurti and Subrahmanyam 1982, Goswani 2005). Several theories have been
12	suggested to explain this observation:
13	1) Northward propagation as a result of feedback between the hydrological cycle and
14	the dynamics over India (Webster 1983). Land sensible heat flux in the boundary
15	layer can destabilize the atmosphere ahead of the ascending zone, causing
16	northward shifts in the convective region;
17	2) The interaction between equatorial moist KW and the monsoon flow can generate
18	(in numerical experiments) unstable quasi-geostrophic baroclinic waves in the
19	monsoon region, weakening the equatorial disturbance (Lau and Peng 1990);
20	3) In a model, continuous NW propagating Rossby waves are seen to emanate from
21	an equatorial KW as it crosses the maritime continent, creating the northward
22	moving rainbands (Wang and Xie 1997);

4) Examination of the poleward propagating rainbands in a high resolution cloud system resolving model indicates that poleward propagation may be due to
 convectively coupled beta drift of low-level vorticity anomalies (Boos and Kuang
 2010).

It seems likely that the poleward propagating modes originate from the same disturbance
as the eastward propagating MJO (e.g. Lawrence and Webster 2002, Jiang *et al.* 2004).
However, it is often observed that the poleward and eastward disturbances separate over
the Indian Ocean and may propagate independently.

9 In this paper, we describe the observation and MSE budget analysis of an MJO-like 10 disturbance in the Super-Parameterized CAM (SPCAM) on a zonally symmetric 11 aquaplanet. This work differs from similar, previous analyses in several ways. Firstly, our 12 analysis is of a model using a more explicit representation of convection - the super-13 parameterization (described below). This improves aspects of the realism of the 14 simulation. Secondly, we use a zonally symmetric basic state, which simplifies the 15 analysis and diagnosis of the energy budget. Thirdly, the MJO observed in our model 16 shows both eastwards and polewards propagation - a phenomenon not reported in earlier 17 works - which allows us to investigate another aspect of the intraseasonal dynamics 18 (albeit in simplified form).

In section 2, the model and the experimental setup is described. Also, basics of the model output are analyzed: Time-space spectra are used to identify the MJO-like signals in the model, which are also visualized in Hovmöller diagrams of the tropics. Towards an understanding of the processes involved in this signal, we present a composite evaluation

1	of the leading terms of the MSE budget of MJO-like signals in Section 3 and their
2	impacts on the MJO-like disturbance's growth and/or propagation are discussed. Further
3	discussion follows in section 4, with conclusions in section 5.
4	2. Model Description
5	a. SPCAM, forcing and Boundary Conditions
6	In this paper, we analyze output from SPCAM version 3.5. SPCAM is a modified version
7	of the Community Atmosphere Model (CAM) where a small domain two-dimensional
8	Cloud System Resolving Model (CSRM) is embedded within each grid point of CAM
9	(Khairoutdinov and Randall, 2001; Khairoutdinov et al., 2005). We use the version of
10	SPCAM with semi-Lagrangian advection at T42 resolution for the CAM component. The
11	model outputs have horizontal resolution of $\sim$ 2.8 degrees. The embedded 2D CSRM is
12	oriented in the north-south direction and has 32 grid points in the horizontal with a 4km
13	resolution. There are 28 vertical levels in the CSRM aligned with the lower 28 vertical
14	levels (out of 30) in the CAM model. The CAM time step is 15 minutes and the CSRM
15	time step is 20 seconds.

16 The model is forced with a temporally and zonally constant Sea Surface Temperature 17 (SST) given as a function of latitude  $\phi$ , in degrees, by:

18 
$$SST(\phi) = 2 + \frac{27}{2}(2 - \zeta - \zeta^2),$$

19 where the SST is in Celsius and

$$\zeta = \begin{cases} \sin^2 \left( \pi \frac{\phi - 5}{110} \right) & 5 < \phi \le 60\\ \sin^2 \left( \pi \frac{\phi - 5}{130} \right) & -60 \le \phi < 5\\ 1 & |\phi| < 60 \end{cases}$$

1

- 2 (plotted in figure 1a), and seasonally varying insolation for sixteen years, with output
  3 every three hours.
- 4

# b. Simulated Climate

5 The model described produces a climate that is qualitatively similar to the central and 6 east Pacific. Some interesting climate quantities are plotted in figure 1. The SST 7 distribution used, which peaks at 5°N, produces a single Inter-Tropical Convergence 8 Zone (ITCZ) in the time mean, with strong precipitation peaked at around  $5^{\circ}$ North (figure 1b), and secondary peaks in the storm tracks at around 40° North and South. 9 10 The ITCZ is also the region of greatest column integrated water (WVP; figure 1c) and 11 low-level zonal winds (U850; figure 1d) within the tropics. The U850 field shows 12 easterlies throughout the tropics, with strongest winds on the edges of the ITCZ. The 13 time/zonal mean low-level meridional wind is weak, but it shows convergence into the 14 ITCZ and the tropics (not shown). The presence of the zonal easterlies in the tropics is a 15 significant deviation from the climate in the region around the warm pool on Earth, 16 where mean westerlies are observed. It is expected that, all else being equal, this will lead 17 to surface flux anomalies that are significantly different to those on the Earth, as the sign 18 of the WISHE effect is dependent upon the signs of both the mean state and anomalous

1	winds. While the presence of a warm pool in the imposed SST can generate a more
2	realistic wind distribution with zonal westerlies, we have chosen to use a simpler setup
3	for this initial investigation.

While the low-level extra-tropical winds are stronger in the Northern Hemisphere, the Southern Hadley Circulation is stronger (not shown). The associated Southern jet is also stronger and more equatorial than the Northern one. This is consistent with the SST boundary condition and explains the strong SH extra-tropical anomalies. It is only at very low levels that the NH winds are slightly stronger.

9

#### c) Moist Static Energy Calculation

10 MSE (denoted by h) in our analysis will be defined as:

11 
$$h = c_p T + g Z + L_v q - L_f q_i$$
 (1)

where T is temperature,  $c_p$  is the specific heat at constant pressure, Z is the height, g is the 12 13 gravitational acceleration,  $L_v$  and  $L_f$  are the latent heats of vaporization and sublimation 14 (at  $0^{\circ}$ C), and q and  $q_i$  are the specific quantities of water vapor and ice respectively. This 15 quantity is sometimes referred to as Frozen MSE. As constructed, the MSE is conserved 16 under phase changes between the solid, liquid, and vapor phases of water and removal or 17 addition of liquid water, all under hydrostatic motion. As a consequence, the column 18 integral of  $h_{\lambda}(h)$ , is approximately conserved in reality and in our model under 19 convective adjustments.  $\langle x \rangle$  represents the mass-weighted vertical integral of quantity x:

$$20 \quad \langle x \rangle = \frac{1}{g} \int_{p_{top}}^{P_{surface}} x dp, \tag{2}$$

where the integral runs from some defined top of the atmosphere (for sufficiently high
tops, the results do not depend upon the precise value chosen) to the surface and g is the
gravitational acceleration. The residual terms arising from non-MSE-conserving effects
are generally small compared to other energy budget terms and can usually be neglected.
(e.g. Neelin and Held 1987, Peters *et al.* 2008).

6

#### d) Spectral Analysis of Model Fields

7 The model equatorial precipitation shows a number of statistically significant peaks 8 representing propagating disturbances (fig 2), when analyzed in zonal wavenumber-9 frequency space, just as observed in OLR from the satellite record (Wheeler and Kiladis 10 1999). These waves represent a large part of the tropical synoptic-scale convective 11 variability, organizing individual convective elements (typically 100 km across, 12 persisting for a few hours) into wavepackets with large spatial (thousands of kilometers) 13 and temporal (days) scales (e.g., Chang 1970; Nakazawa 1988). The wave activity peaks 14 have been identified with the equatorially trapped waves of rotating shallow water wave 15 theories (e.g., Matsuno 1966; Wheeler and Kiladis 1999; Yang et al. 2007, Andersen and 16 Kuang 2008). Not present in the classical shallow water wave system, and missing from 17 most simple models is the large signal at intraseasonal (30-90 days) timescales and zonal 18 wavenumbers 1-3 that is the spectral signal of the MJO.

Figure 2a shows the precipitation power spectrum for disturbances symmetric about the
equator. This is constructed following the procedure of Wheeler and Kiladis (1999).
These spectra are broadly similar to observations, with strong MJO, KW, and Rossby
wave signals. The equivalent depth (a measure of the vertical scale of the wave structure,

1	inferred from the phase speed) is approximately 25m, similar to that observed. SPCAM,
2	with a generally similar SST distribution, has previously been shown to possess MJO-like
3	spectral features (Marat Khairoutdinov, personal communication).
4	The antisymmetric part of the SPCAM spectrum (not shown) is not as realistic. For
5	example, the Mixed Rossby-Gravity (MRG) waves are not well represented. However,
6	we have observed that this feature is stronger in double ITCZ mean states. The mean state
7	dependence of the features of the spectrum is an interesting and open question that we do
8	not address here.
9	The spectrum of OLR (not shown) is generally similar. The spectra of MSE disturbances
10	(figure 2b) are different to the precipitation and OLR spectra – the Kelvin and Rossby
11	waves are weaker, while the MJO signal remains strong relative to the background (this
12	is also seen in the observed spectra of precipitable water, e.g. Roundy and Frank 2004,
13	Yasunaga and Mapes 2011). This is another indication that the MJO is a fundamentally
14	different type of wave to the KW – one that is dominated by MSE fluctutions, rather than
15	the buoyancy fluctuations that drive the shallow water wave type behaviour of the other
16	waves. The MSE spectrum also includes a number of peaks around wavenumber 6. These
17	are the signature of the strong extratropical waves present in our model entering the
18	equatorial region. Care must be taken to exclude these waves from our MJO signatures
19	used for the regression studies below.
20	In order to demonstrate that the column MSE anomalies are a fundamental part of the
21	MJO-like disturbance rather than simply being generated by it, we have conducted an

22 experiment where the column MSE in the model (between  $20^{\circ}$ N- $20^{\circ}$ S) is damped

1	towards its time- and zonal-mean values with a 12-hour timescale. To maintain the
2	climatology, the zonally averaging prognostic variables (excluding temperature) are
3	nudged to the climatological values of the control runs over a timescale of 30 minutes.
4	Temperature is nudged weakly with a timescale of 10 days. We have verified that
5	nudging alone, without adding the column MSE damping, produced a spectrum similar to
6	that of the control experiment. In this case, while the Kelvin waves are still present in the
7	simulated precipitation, the MJO-like signal is greatly reduced (figure 2c). Figure 2d
8	shows an experiment where radiative heating is homogenized in the zonal direction. The
9	results of this experiment are discussed in below.
10	Figures 3a and figure 3b shows equatorial $(0^{o}-6^{o}N)$ Hovmöller plots of precipitation for
11	a short period of our model run. Even in the unfiltered field (figure 3a), a strong MJO
12	event can be seen propagating eastwards, beginning at ~300E and Day 5600, continuing
13	around the globe coherently for at least two full circumferences over a period of
14	approximately 120 days. The multi-scale nature of the MJO in the model can be seen in
15	this field - the MJO envelope contains and modulates many faster moving, short-lived
16	waves traveling in both easterly and westerly directions.
17	Once the precipitation is filtered into the MJO frequency and wavenumber region of
18	spectral space (wavenumbers 1—3, periods 20—100 days), the MJO signal is easily seen

(figure 3b). MJO events tend to arise randomly, propagate for 1-2 circumnavigations and
then die off, while another event arises elsewhere on the globe. The mechanisms involved
in the events' beginnings and ends are beyond the scope of the current work and will not

22 be investigated in this paper.

1	Poleward propagation can also be observed in the precipitation field. Figure 3c shows the
2	time-latitude evolution of precipitation, averaged over 160°E to 160°W. Poleward
3	propagating signals can be seen to move from near the equator to up to $25^{\circ}$ N.
4	3. Results
5	a) Regression Technique
6	To look at the structure of the MJO disturbances, we regress unfiltered model fields
7	against the MJO filtered OLR field, with the following procedure:
8	1)Model OLR is filtered to the MJO spectral region $(1 \le k \le 3, 0.01/day \le f \le 1)$
9	0.05/day), in the fashion of Wheeler and Kiladis (1999), using a time-space Fourier
10	transform followed by masking to the MJO region and then an inverse Fourier transform.
11	The spectral region chosen is narrower than that used in Wheeler and Kiladis (1999) in
12	order to reduce the contamination of the MJO signal by the very strong extra-tropical
13	waves.
14	2)The time variance of the filtered OLR is calculated at each point and we identify
15	the latitude that has the largest zonal mean variance – all of the reference points will
16	come from this latitude. The reference latitude for the mean state considered is 4.2°N, the
17	location resolved with the model closest to the peak SST
18	3)We concatenate the filtered OLR time series for every point on the latitude chosen
19	as our reference. This allows us to use the MJO from all parts of the globe to construct
20	our regression improving the signal-to-noise, although it also introduces complications

1 due to the various correlations in the fields.

*4)*The model fields are similarly concatenated into one long time series at each model
point, appropriately circle shifted so that the spatial relationship with the reference points
is maintained.

5 5)For each field of interest, at each spatial point in the model we estimate a regression
coefficient, b – the slope of the model fields at that point versus the reference MJO OLR
time series – using standard least-squares linear regression (e.g. Wilks 2006).

8 6)We consider the regression results statistically significant at each point if the null 9 hypothesis (b = 0) can be rejected at the 95% confidence level for that point. For this 10 purpose, we calculate confidence ranges for the slopes, by estimating the standard 11 deviation,  $\sigma$ , of the population the slope is drawn from (again, through the standard 12 techniques of least-squares linear regressions e.g. Wilks 2006). As there are time and 13 space correlations in the various fields, we estimate the effective number of degrees of 14 freedom (or independent MJO events) to be ~35000. This accounts for both the time 15 correlations at each point and the spatial correlations between neighboring point's time 16 series. We base this estimate upon observations of a correlation time of approximately 4 17 days and correlation length of approximately 8 degrees in the unfiltered fields such as 18 zonal wind. We have also made estimates using the larger correlations in the filtered 19 fields; this has little impact on the results that we present. We assume that the population 20 of slopes has a Gaussian distribution, then the 95% confidence interval spans a region 21 almost two standard deviations from the slope *b*:

$$b_{range} = b \pm 1.92 \times \sigma$$

1 Points where the null hypothesis cannot be sufficiently rejected are discarded.

7) The regression coefficients that pass the significance test are multiplied by a
typical OLR peak anomaly (-40W/m<sup>2</sup>), to give the magnitudes of the field anomalies
associated with an MJO event.

This regression technique focuses on the mature phase of the MJO-like disturbance,
which is, due to the zonal symmetry, the dominant phase in our model. The relationships
between the model fields and the disturbance could be quite different during the initiation
and decay phases of the disturbance.

9

#### b) Dynamic field regressions

The model fields are regressed against the MJO-filtered OLR on the latitude of greatest mean variance as described above to show the structure of the MJO-like disturbance in the model. Several model fields are shown in figure 4. The regression basis point at (180E, 4.2N) is indicated on the figures and the coastlines are included in the map to give a sense of the scale of the disturbances.

The composite MJO's convective signal can be seen in the OLR field (figure 4a) – which is essentially a measure of the average temperature of the highest opaque surface visible to the satellite. There is a large region of reduced OLR around the regression point, caused by colder emissions from the larger number of higher cloud tops in the active phase. The suppressed convection is visible as the warm anomalies, which are caused by the warmer temperatures of the low cloud tops and the greater lower-troposphere and sea surface area visible from space in this region.

1 Precipitation (figure 4b) is likewise enhanced near the regression point and suppressed to 2 the east and west of the convective signal, although the enhancement is much stronger in 3 the region of the ITCZ where the mean conditions are much more conducive to 4 precipitation (and the mean precipitation is larger). The enhanced precipitation also 5 possesses a noticeable tilt, with the eastern edge closer to the equator and the western 6 edge closer to the pole. The convective region also contains a positive moisture anomaly, 7 seen as an increase in the integrated column moisture (figure 4c), that has a tilt similar to 8 the precipitation. The large moist anomalies in at around 120°W, 40°N and 40°S are due 9 to the advection of moist tropical air by the MJO large-scale low-level winds. Similarly, 10 the smaller dry anomaly at  $\sim 160^{\circ}$ E,  $30^{\circ}$ S is due to the advection of dry extratropical air 11 into the tropics by the MJO large-scale flow.

The OLR signal has a greater spatial extent than the precipitation. This is not considered surprising, as we expect that the OLR anomalies can be generated by modification in the amount or depth of convection throughout the tropics, while the precipitation anomalies are expected to be larger where the mean state conditions are more favorable for precipitation i.e. within the ITCZ.

The wind fields (850 hPa - figure 5a - and 200hPa - figure 5b) show circulation similar to that typical of the MJO, with low-level convergence near the convective center and divergence centered approximately halfway around the planet. The upper-level winds show a reversed pattern, with divergence above the reference point. The peak low-level winds are located near the ITCZ. While the westerlies peak to the west of the convective center, there is a small westerly signal under the convection. Also visible at low levels are the Rossby gyres associated with the MJO (e.g. Weickmann 1983, Hendon and Salby

1	1994, and Kiladis et al. 2005). However, the upper level gyre visible in the southern
2	hemisphere is not the tropical response to the MJO heating. This gyre is located
3	significantly closer to the equator, and the gyre is seen to tilt toward the pole with height,
4	as seen in observations. In figure 5c, we can see the zonal wind structure at the reference
5	longitude. The poleward tilt and the baroclinic nature of the gyre are visible near the
6	equator. The gyre visible in the vector fields is due to the interaction with the
7	extratropical response in the Southern jet, in the form of an equivalent barotropic gyre,
8	which adds to the baroclinic tropical gyre to create the observed wind field.
9	The regressed fields also show strong signals of extra-tropical waves, present in the
10	strong jets within the model. To the south of the equator, these signals can be quite
11	prominent and quite equatorial due to the stronger southern Hadley Cell.
12	c) MSE budget and residual calculations
12 13	c) MSE budget and residual calculations The MSE is calculated every three hours from the model instantaneous fields. The 3D
12 13 14	c) MSE budget and residual calculations The MSE is calculated every three hours from the model instantaneous fields. The 3D MSE field and the column integrated MSE are regressed against the MJO index to give a
12 13 14 15	c) MSE budget and residual calculations The MSE is calculated every three hours from the model instantaneous fields. The 3D MSE field and the column integrated MSE are regressed against the MJO index to give a composite structure of the MSE anomalies associated with the MJO. Much like
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<ol> <li>12</li> <li>13</li> <li>14</li> <li>15</li> <li>16</li> <li>17</li> <li>18</li> <li>19</li> <li>20</li> </ol>	c) MSE budget and residual calculations The MSE is calculated every three hours from the model instantaneous fields. The 3D MSE field and the column integrated MSE are regressed against the MJO index to give a composite structure of the MSE anomalies associated with the MJO. Much like observations of the Earth's MJO, the observed anomalies have a tilted vertical structure (figure 6a), with preconditioning of the lower and middle troposphere ahead (east) of the convective signal (Kiladis <i>et al.</i> 2005). This MSE anomaly is dominated in the low and middle troposphere by the moisture anomaly (not shown) associated with the signal. The peak MSE anomaly in the model is approximately 2 kJ/kg, in approximate agreement
<ol> <li>12</li> <li>13</li> <li>14</li> <li>15</li> <li>16</li> <li>17</li> <li>18</li> <li>19</li> <li>20</li> <li>21</li> </ol>	c) MSE budget and residual calculations The MSE is calculated every three hours from the model instantaneous fields. The 3D MSE field and the column integrated MSE are regressed against the MJO index to give a composite structure of the MSE anomalies associated with the MJO. Much like observations of the Earth's MJO, the observed anomalies have a tilted vertical structure (figure 6a), with preconditioning of the lower and middle troposphere ahead (east) of the convective signal (Kiladis <i>et al.</i> 2005). This MSE anomaly is dominated in the low and middle troposphere by the moisture anomaly (not shown) associated with the signal. The peak MSE anomaly in the model is approximately 2 kJ/kg, in approximate agreement with observed values (e.g., Kemball-Cook and Weare 2001; Kiladis <i>et al.</i> 2005).

integrated moisture field (Figure 4c) – as moisture anomalies dominate the column MSE
anomalies at the MJO timescale – with a positive MSE anomaly running approximately
along the ITCZ region, with the western end tilted polewards.

The column integrated MSE tendency is calculated in two ways. We can calculate it
indirectly from the column integrated budget terms from the time mean fields over that
three-hour interval:

7 
$$\langle \partial_t h \rangle_{budget} = -\langle \omega \partial_p h \rangle - \langle v \cdot \nabla h \rangle + LH + SH + \langle LW \rangle + \langle SW \rangle,$$
 (3)

where p is the pressure, v is the pressure-surface wind vector, ω is the pressure velocity,
LH and SH represent the latent and sensible heat fluxes into the atmospheric column
from the surface, and LW and SW are the long- and short-wave radiative heating rates.
The left-hand side is the local tendency of (h), the first and second terms on the right
represent advection of h by the winds, and the final four terms represent the external
sources.

14 The MSE tendency can also be calculated directly by subtracting the MSE at the last time 15 step from the current value before vertically integrating:

16 
$$\langle \partial_t h \rangle_{explicit} = \langle \frac{h(t) - h(t - \Delta t)}{\Delta t} \rangle$$
 (4)

Both these tendency terms are calculated explicitly from the eight times daily output of
SPCAM and then regressed against the MJO OLR as described above, allowing us to
determine their contributions to the MJO-like signal's MSE tendency.

20 The calculated budget for the MJO-like anomalies shows positive MSE tendencies to the

1	east and to the north of the convective center with negative anomalies to the west and
2	equatorwards. This distribution indicates that the MSE anomaly is propagating to the east
3	and towards the pole (figure 6c).
4	The difference between the two $\langle \partial_t h \rangle$ values is the residual, and is a combination of
5	numerical effects, processes that slightly violate conservation of MSE, and errors due to
6	phenomena happening at time- and space-scales smaller than the scales in the output data
7	The residual is also regressed against the MJO OLR to determine its contribution to the
8	MSE budget for the MJO (Figure 6d). For the small number of points where it is
9	statistically significant, the regressed residual is generally small compared to the leading
10	h tendency terms, allowing us to have some confidence in our diagnosis of these terms'
11	contribution to the MSE budget for the MJO.

#### 12 d) Decomposition

By projecting anomalies in the budget quantities onto the MSE anomaly and its time derivative, we can determine which terms contribute most to the maintenance/dissipation of the anomaly and which contribute to/retard the propagation. In figure 7a, the fractional energy source for the MSE anomaly due to each term is displayed (sensible heat flux is negligible and not plotted). The contribution due to source x,  $S_x$ , is calculated as

$$S_x = \frac{\|x \cdot \langle h \rangle\|}{\|\langle h \rangle^2\|}$$

18 where  $||y|| = \iint_{ITCZ} y dA$  is the integral over the ITCZ (6°S to 12°N here, along all 19 longitudes) of quantity y. In this case, the "ITCZ" is defined as the region where 1 precipitation is both strong and varies approximately linearly with column MSE.

2 From this we can see, firstly, that the MSE tendency is almost exactly in quadrature with 3 the MSE anomaly, which is to be expected from the fashion in which we constructed the 4 composites. We can also see that the long-wave heating,  $\langle LW \rangle$ , is the dominant source of 5 column MSE for the MJO, with a small contribution from the short-wave heating,  $\langle SW \rangle$ , and the residual processes. The other terms shown - horizontal advection,  $\langle \vec{V} \nabla h \rangle$ , vertical 6 7 advection,  $\langle \omega \partial_{p} h \rangle$ , and the latent heat flux, LHF, are all net sinks of column MSE. The 8 sum of the sources is shown, for comparison with the projection of dh/dt. The difference 9 is negligible compared to the sources shown.

10 The contribution each term x makes to the propagation,  $s_x$ , is shown in figure 7b. This is 11 calculated in a similar way to the contribution to the anomaly:

$$s_x = \frac{\|x \cdot \langle dh/dt \rangle\|}{\|\langle dh/dt \rangle^2\|}$$

As can be seen, the long-wave is the only significant retarding quantity, while both
advection terms are significant sources of MSE associated with the propagation of the
anomaly.

Comparison of the amplitude of the regression coefficients in the MSE budget (equation
3) allows us to identify the leading terms in the MJO MSE budget for this experiment.
These are:

18 i. Long-wave heating (figure 8a) – The long-wave heating anomaly, caused primarily by
19 the anomalously low OLR from the enhanced anvil clouds, acts as a source of column

1	integrated MSE variability, balanced against the sinks due to the vertical and horizontal
2	advection and latent heat flux anomalies in the region around the convective center.
3	The long-wave heating anomaly is approximately 26% of the precipitation anomaly (in
4	power units) at the regression point, larger than that observed by Lin and Mapes
5	(2004). To demonstrate the importance of the long-wave heating to our observed
6	anomaly, we have conducted a mechanism denial experiment, wherein the radiative
7	heating is homogenized zonally, while the climatology is maintained through the same
8	methods as the MSE damping experiment described above. In this case (figure 2d), we
9	observe that the Kelvin waves are still active, while the MJO-like disturbance is absent
10	from the precipitation spectrum.
11	ii. Horizontal advection (figure 8b) – Horizontal advection acts as a source of column
12	MSE to the east and especially polewards of the convective center. The horizontal
13	advection term is discussed in more detail below.
14	iii. Vertical advection (figure 8c) – Vertical advection of MSE appears to be a source of
15	column integrated MSE to the east of the convective center, in the suppressed region,
16	and a sink of column MSE in the convective region. This causes it to act as a damping
17	on the anomaly. There is also a significant overlap between the vertical advection and
18	the column MSE tendency, contributing to the eastward propagation. Vertical
19	advection also appears to act against the polewards propagation, by counteracting some
20	of the energy import by horizontal advection in the region polewards of the convective
21	center. The Normalized Gross Moist Stability (NGMS) is defined as

22 
$$NGMS = \frac{\langle \omega \partial_p h \rangle}{P},$$

1 where P is the precipitation anomaly in power units. For the composite disturbance in 2 SPCAM, the NGMS at the regression point is approximately 0.21. NGMS is a measure of 3 the efficiency with which the divergent flow exports MSE. A positive value represents 4 stability, although a small value is more easily overcome by other mechanisms, such as 5 the long-wave heating discussed previously. The NGMS could decrease with horizontal 6 wavelength (e.g. Kuang 2011), contributing to the scale selection of the MJO-like 7 distrubances. Whether this wavelength dependence is the case in our present experiments 8 is not clear. 9 The column integrated MSE variability source represented by the advection at around  $30^{\circ}$  to  $40^{\circ}$ N is substantially polewards of the MSE tendency – this appears to be a signal 10 11 of the extratropical waves that are strong in this model, rather than the MJO. The 12 extratropical waves appear at the northern edge of the analysis domain as large signals in 13 horizontal and vertical advection. These sources mostly cancel together as shown by the 14 total advection, in figure 8d. 15 Surface latent heat flux (figure 9a) has a small contribution to the MSE anomaly 16 propagation. However, as latent heat flux anomaly is a significant sink of column 17 integrated MSE variability from the anomaly, this term deserves some investigation. The

18 LHF anomaly is mostly negative under the positive column MSE anomaly, leading to

19 damping of the MJO by LHF. This is not totally consistent with the simple WISHE

20 picture and the mean state easterlies that exist near the equator.

21 The latent heating distribution observed can be explained in terms of a bulk surface flux

22 formulation, which is a reasonable approximation for the surface scheme used in

1 SPCAM,

2 
$$LHF = C |\overrightarrow{u}| (q^* - q_{sfc}),$$
 (5)

where C is a constant;  $|\vec{u}|$  is the windspeed near the surface;  $q^*$  is the saturation humidity at the surface temperature and pressure; and  $q_{sfc}$  is the actual humidity near the surface. In the WISHE argument, the changes in  $|\vec{u}|$  across a disturbance are assumed to dominate changes in LHF. The climate-zonal mean latent heat flux calculated with equation 5 is qualitatively the same as that calculated by the model surface scheme (not shown). In this calculation, C is estimated by finding the multiplier that minimizes the difference between the two time-zonal mean LHF curves.

In the bulk surface flux calculation, the flux anomalies can be linearly approximated by a
sum of flux anomalies due to the various anomalies in the dynamic fields associated with
the MJO:

13 
$$LHF \approx C |\overrightarrow{u}| (q^* - q_{sfc}) + C\Delta |\overrightarrow{u}| (q^* - q_{sfc}) - C |\overrightarrow{u}| (\Delta q_{sfc}) + C |\overrightarrow{u}| (\Delta q^*), (6)$$

The first term on the right is the mean LHF, the second is the anomaly due to the changed wind speed as the MJO passes (figure 9b); the third term is the flux anomaly due to the change in moisture as the MJO passes (figure 9c) and the last term is the anomaly due to the change in surface saturation humidity due to the surface pressure anomalies of the MJO (not shown) which is negligible compared to the other terms.

As can be seen, the surface latent heat flux anomaly of the MJO is not purely determinedby the wind speed anomaly. For example, the negative LHF anomaly to the northeast and

1	southeast of the convection is dominated by the moisture anomaly due to the MJO scale
2	circulation carrying moist equatorial air into the dryer regions outside the ITCZ. In these
3	regions the wind speed anomalies are relatively small. On the other hand, the heating
4	along the equator, west of the center, is largely due to the increased wind speed there, as
5	the moisture anomaly near the surface is small in that region. As a third example, the
6	weak negative anomaly to the west-northwest is due to the competition between a
7	substantial slowing of the winds and a dry anomaly due to moisture advection. The
8	reverse is also true to the east-north-east.
9	It is important to note that this decomposition should only be considered as a qualitative
10	explanation of the flux anomalies, as the sum of the bulk flux derived anomalies does not
11	match the actual flux anomaly quantitatively (compare figure 9a and figure 9d).
12	Due to the relative phases of the various terms, it appears that the propagation, especially
13	the polewards part, is significantly driven by the horizontal advection of MSE, so we will
14	now focus our attention on that term to gain further insight into the MJO propagation

15 mechanisms.

16 e) Decomposition of horizontal advection into zonal and meridional advection:

- 17 While the advection in the model is Semi-Lagrangian, it can be approximately
- 18 decomposed into zonal (hadv<sub>Z</sub>) and meridional (hadv<sub>M</sub>) contributions:

$$19 \quad \begin{array}{l} hadv_{Z} = -\langle u\partial_{x}h \rangle \\ hadv_{M} = -\langle v\partial_{y}h \rangle \end{array}$$
(7)

20 As can be seen in figure 10a, the zonal advection acts as a source of MSE to the northeast

of the convective center. However, as discussed above, much of this MSE tendency is due to extratropical wave activity and is largely balanced by the vertical advection associated with the waves in the same area. The meridional MSE advection anomaly (figure 10b) also acts as a source of column integrated MSE to the east and to the northeast of the convective center and as a sink under the convective center and to equatorwards. This acts to propagate the MSE anomaly both eastwards and polewards.

# 7 f) Timescales of Meridional Advection

8 The meridional advection can be further divided into the contributions from various9 timescales:

$$10 \quad -\langle v\partial_y h \rangle = -\langle v_{hf}\partial_y h_{hf} \rangle - \langle v_{lf}\partial_y h_{lf} \rangle - \langle v_{hf}\partial_y h_{lf} \rangle - \langle v_{lf}\partial_y h_{hf} \rangle \tag{8}$$

11 where the subscripts *hf* indicates time filtered to periods T < 30 days; and *lf* indicates 12 T>30 days.

Each of the four product terms is regressed against the MJO OLR signal. The dominant term,  $\langle v_{hf} \partial_y h_{hf} \rangle$ , is shown in figure 10c. The remaining terms (not shown) are much less significant for the MJO-like signal. This figure shows a source of MSE to the northeast of the convective center, and a sink at the center, to the west, and to the northwest. This term dominates the total meridional advection to the energy source in the northeast, and so seems to dominate the polewards part of the propagation of the MJOlike signal and is a significant part of the eastward propagation.



$$D \approx \kappa \nabla^2 \langle h \rangle$$
,

1 where D is the diffusive source and  $\kappa$  is the eddy diffusion. To linear order, the eddy

- 2 diffusion can be broken into the diffusion of the mean MSE profile by the MJO-
- 3 associated eddy anomalies and the diffusion of the MJO MSE anomalies by the mean
- 4 eddy activity. As a simple, dimensionally consistent, approximation,  $\kappa$  can be considered
- 5 to be proportional to the square root of the Eddy Kinetic Energy (EKE):

6 
$$\kappa = \bar{\kappa} + \kappa' \propto (\overline{EKE} + EKE')^{0.5}$$
.

7 Expanding this to first order yields

$$\kappa' \propto \frac{1}{2} \frac{EKE'}{\overline{EKE}^{0.5}}$$

8 The diffusion can then be written as:

$$D \propto \frac{1}{2} \frac{EKE'}{\overline{EKE}^{0.5}} \nabla^2 \overline{\langle h \rangle} + \overline{EKE}^{0.5} \nabla^2 \langle h \rangle',$$

9 where the primed quantities are associated with the MJO and the overbar indicates the 10 climate mean quantities. These two quantities are shown as figures 11a and 11b. The first 11 term is the diffusion of the mean MSE by the eddies associated with the MJO. The 12 second term is the diffusion of the MJO MSE anomalies by the mean eddy activity. 13 As can be seen over the ITCZ latitudes, the MJO eddy term matches the meridional eddy 14 MSE advection term to the east of the convection indicating that the MJO associated 15 eddies are responsible for the meridional eddy advection in that region and thus provides 16 the meridional advection's contribution to the eastward propagation. The mean eddy

diffusion of the MSE anomaly, on the other hand, seems to be responsible for the
advection to the north-east of the convection. Thus the gradients in the MJO MSE
anomaly drive the poleward propagation of the MJO. The sum of the two diffusion terms
is shown in figure 11c. The close correspondence between this and the eddy meridional
advection (figure 10c) demonstrates the validity of representing the eddy advection terms
as eddy diffusion, also shown to be the case in reanalysis data (Peters *et al.* 2008).

7 On the whole, what we seem to be seeing is a suppression of high-frequency eddy drying 8 in the lower troposphere to the east of the convective center, and enhancement of the 9 eddy drying to the west (figure 12a), in combination with MSE anomalies interacting 10 with the mean eddy activity to create moistening to the northeast of the convection and 11 drying near the convection. The vertical structure of the EKE anomaly (figure 12b) at 12 15°N shows the suppression of eddy advection in the lower troposphere ahead of the 13 convection, collocated with the anomalous moistening. Likewise, a positive EKE 14 anomaly is collocated with anomalous drying. A similar picture emerges at 5°N, where 15 the anomalous moistening is closely tied to the suppressed EKE (figures 12c & 12d).

16 Figure 13a shows the 850hPa EKE anomaly, which can be seen to have a strong negative 17 relationship to the column eddy meridional moisture advection anomaly (figure 10b). 18 This relationship generally holds for the lower troposphere. The upper-level EKE 19 anomalies generally have the opposite sign to the lower troposphere, but as the moisture 20 gradient in the upper atmosphere is very small, the advection anomalies from the upper 21 troposphere have a negligible influence upon the column integrated MSE. This is in 22 agreement with observations of the eddy activity in the tropics, where the eddy kinetic 23 energy is reduced in the MJO easterlies and enhanced in the MJO westerlies, dominated

1 by barotropic conversion terms (e.g. Maloney and Hartmann 2001, Maloney and

2 Dickinson 2003). Barotropic conversion moves mean flow energy into eddy energy,

3 caused by eddy advection of gradients in the large-scale winds. The tendency of EKE due

4 to barotropic conversion is given by

5 
$$\partial_t EKE_{barotropic} = -u_{hf}v_{hf}(\partial_y u_{lf} + \partial_x v_{lf}) - u_{hf}^2 \partial_x u_{lf} - v_{hf}^2 \partial_y v_{lf}$$
 (9)

6 where  $(u_{hf}, v_{hf})$  is the high frequency wind and  $(u_{lf}, v_{lf})$  are the low frequency winds. 7 Figure 13b shows the MJO regressed generation of EKE by barotropic conversion (the 8 right-hand side of the above equation), also at 850 hPa. As can be seen, extra EKE is 9 generated by barotropic conversion in region around the convective center and to the 10 west and northwest. EKE is reduced by the negative barotropic conversion anomaly in 11 the region to the east of the convective center, consistent with the observations (e.g. 12 Maloney and Hartmann 2001, Maloney and Dickinson 2003).

# 13 4. Discussion

Many attempts have been made to explain the tropical OLR spectrum as coming from a system of convectively coupled shallow water waves. However, the current results take the view that the MJO disturbance is of a fundamentally different nature, stemming from anomalies in column MSE, rather than from anomalies in Convective Available Potential Energy (CAPE) and/or other similar quantities caused by the temperature anomalies of the waves, as seems to be the case for the convectively-coupled equatorial shallow water waves observed.

21 To correctly model the MJO, it appears that a simple model must account for these

1 effects. More specifically, because the horizontal advection of MSE due to meridional 2 winds – and anomalies in this caused by variations in barotropic conversion – appears to have such a significant effect on the MJO mode, both the influence of these anomalies on 3 4 the convection and the feedback on these effects by the large-scale flow induced by the 5 MJO convection ought to be included. 6 We have also observed that surface thermodynamic disequilibrium caused by moisture 7 anomalies can be as important as windspeed anomalies in determining the LHF 8 anomalies, at least in the situation modeled in this study. 9 It is worthwhile discussing the ways our results compare to some other investigations of 10 the MJO energy sources. 11 In a modeling study Raymond (2001) investigated the importance of cloud-radiation 12 feedback and surface energy fluxes in the genesis and propagation of the MJO. Raymond 13 observed that Cloud-Radiation feedback was crucial for MJO genesis, while surface heat 14 fluxes were important for propagation. In the present analysis we do not investigate the 15 genesis of the MJO events, but we do observe that cloud-radiation interactions (in the 16 form of long-wave heating anomalies) are a major part of the MSE budget for the 17 maintenance of the disturbance. Surface heat fluxes do not play a significant role in the 18 propagation of the MJO-like anomaly we observe. 19 Raymond also observes that a mean state similar to that above the warm pool is critical to 20 the existence of the MJO. However, we have observed the MJO in our zonally symmetric 21 SPCAM experiment. It is not clear whether this observation is a strength or a weakness of

22 SPCAM.
1	Lin and Mapes (2004) investigated the radiation budget of the MJO based upon
2	observations from the Atmospheric Radiation Measurement (ARM) program and the
3	Tropical Ocean Global Atmosphere Coupled Ocean Atmosphere Response Experiment
4	(TOGA COARE) campaign. They observed that the net column radiative heating is
5	almost in phase with the precipitation. We observe a similar phase relationship in
6	SPCAM, where the radiative heating is approximately in phase with the MSE anomaly,
7	with a slight lag indicated by the retarding effect of the long wave term. In both Lin and
8	Mapes and the present work, the radiative heating anomaly is dominated by the long
9	wave anomaly that results from changes in the high clouds by the MJO modulation of
10	convection. The ratio of radiative heating to latent heat release we determine (26%) is
11	significantly larger than the 15% estimated by Lin and Mapes.
11 12	significantly larger than the 15% estimated by Lin and Mapes. Our results are generally consistent with those of Maloney (2009). We see a buildup of
11 12 13	significantly larger than the 15% estimated by Lin and Mapes. Our results are generally consistent with those of Maloney (2009). We see a buildup of column MSE in advance of the precipitation anomaly and a decay of column MSE during
11 12 13 14	significantly larger than the 15% estimated by Lin and Mapes. Our results are generally consistent with those of Maloney (2009). We see a buildup of column MSE in advance of the precipitation anomaly and a decay of column MSE during and after the precipitation. We also observe that the horizontal advection of MSE is
<ol> <li>11</li> <li>12</li> <li>13</li> <li>14</li> <li>15</li> </ol>	significantly larger than the 15% estimated by Lin and Mapes. Our results are generally consistent with those of Maloney (2009). We see a buildup of column MSE in advance of the precipitation anomaly and a decay of column MSE during and after the precipitation. We also observe that the horizontal advection of MSE is among the leading terms in the column MSE budget. However, in contrast to Maloney
<ol> <li>11</li> <li>12</li> <li>13</li> <li>14</li> <li>15</li> <li>16</li> </ol>	significantly larger than the 15% estimated by Lin and Mapes. Our results are generally consistent with those of Maloney (2009). We see a buildup of column MSE in advance of the precipitation anomaly and a decay of column MSE during and after the precipitation. We also observe that the horizontal advection of MSE is among the leading terms in the column MSE budget. However, in contrast to Maloney (2009), we observe that latent heat flux has only a small budget contribution. The long-
<ol> <li>11</li> <li>12</li> <li>13</li> <li>14</li> <li>15</li> <li>16</li> <li>17</li> </ol>	significantly larger than the 15% estimated by Lin and Mapes. Our results are generally consistent with those of Maloney (2009). We see a buildup of column MSE in advance of the precipitation anomaly and a decay of column MSE during and after the precipitation. We also observe that the horizontal advection of MSE is among the leading terms in the column MSE budget. However, in contrast to Maloney (2009), we observe that latent heat flux has only a small budget contribution. The long- wave heating anomaly is observed to be more important in the present work than it
<ol> <li>11</li> <li>12</li> <li>13</li> <li>14</li> <li>15</li> <li>16</li> <li>17</li> <li>18</li> </ol>	significantly larger than the 15% estimated by Lin and Mapes. Our results are generally consistent with those of Maloney (2009). We see a buildup of column MSE in advance of the precipitation anomaly and a decay of column MSE during and after the precipitation. We also observe that the horizontal advection of MSE is among the leading terms in the column MSE budget. However, in contrast to Maloney (2009), we observe that latent heat flux has only a small budget contribution. The long- wave heating anomaly is observed to be more important in the present work than it appears to be in Maloney 2009.

21 by the meridional transport of moisture by synoptic scale eddies. The modulation of the

largely in agreement with that of Maloney 2009. The horizontal advection is dominated

22 eddy activity by the MJO large-scale state leads to modulation of the moisture transport,

23 leading to anomalous moistening and drying effects.

20

1	However, in a follow up paper, Maloney et al. (2010) made a number of observations that
2	are inconsistent with the results we report. Specifically Maloney et al. reports that, in the
3	presence of reduced humidity gradients (i.e. reduced eddy meridional advection effects)
4	and a warm pool SST, the MJO observed is stronger. They further observed, in this
5	configuration, that the propagation of the MSE anomaly was primarily due to zonal
6	advection of moisture by the mean low-level wind. It is important to note, however, that
7	the mean surface westerlies in Maloney et al. (2010) are considerably stronger than those
8	observed over the Indian Ocean and the Western Pacific. We have not addressed the
9	question of whether the mechanisms observed in SPCAM would change in a similar way
10	in the present study, but this is a planned avenue of further research.
11	Poleward propagation of the MJO-like disturbance is demonstrated by the Hovmöller
12	diagram in figure 3. This is not surprising, given the tilted nature of the MSE and
13	precipitation anomalies. The MSE budgets indicate that meridional advection of MSE is
14	important in the poleward propagation of the disturbance, and is likely important in the
15	poleward propagation of similar phenomena on the Earth, such as the Asian Monsoon. In
16	a study by Boos and Kuang (2010), similar poleward propagating intraseasonal anomalies
17	are observed in a nonhydrostatic model with zonally symmetric boundary conditions.
18	These anomalies are seen to propagate through a similar mechanism, through the actions
10	of small goals addies upon the column MSE

## 20 5. Conclusions

By analyzing the column integral, we have glossed over the specifics of how moistconvection in the model redistributes MSE. However, the budget analysis provides a

1	useful framework to assess the importance of various processes. Our arguments, based
2	upon budget analysis, are not intended to show causality. We can, however, see terms
3	that are "important" in various parts of the wave, in the sense that, an important part of
4	the budget is one that would necessitate large changes in the other terms to maintain
5	balance were that term removed. It is also possible to infer from the signs of the
6	important terms some information about how the MSE anomaly would react if a term was
7	removed (eg, moving faster or slower, growing or decaying), at least in a transient sense,
8	before the other terms responded.
9	Our conclusions are:
10	a) The SPCAM run in a zonally symmetric aquaplanet configuration shows an MJO-
11	like feature in both the OLR and MSE spectra.
12	b) This feature is similar to the Earth's MJO in structure and propagation. The
13	composite structure of the MJO-like signal shows enhanced moisture and
14	precipitation in the convectively active region, coupled with a planetary scale
15	circulation. The convective anomaly is preceded by low-level moistening,
16	preconditioning the atmosphere for the convective activity. The anomalies
17	propagate both eastwards at a realistic zonal speed and also polewards, similar to
18	observations.
19	c) There are, however, some aspects of the disturbance that are less like the real-
20	world MJO. Such differences are not surprising in an experiment conducted on an
21	idealized zonally asymmetric aquaplanet set up, but we consider the system worth
22	analyzing. The observation of realistic MJO events observed in experiments

1	conducted in the same model with realistic boundary conditions, lends some
2	confidence that our anomaly is related to the MJO, despite the differences. We
3	believe that the analysis of this idealized experiment can be informative as to the
4	mechanisms that are involved in the MJO maintenance and propagation.
5	d) The composite MJO-like feature appears as a large positive MSE anomaly located
6	over and around the ITCZ and the center of MJO filtered OLR variability. The
7	composite MSE tendency has MSE increasing to the east and polewards of the
8	convective center, and decreasing to the west and equatorwards.
9	e) The primary source of MSE in phase with the observed anomaly is the anomalous
10	long-wave heating, caused by the enhanced deep convection (and reduced mean
11	cloud top/emission temperature) in the convective region of the MJO. This source
12	of energy is balanced by sinks, which are dominated by the advection of MSE. The
13	importance of long wave heating appears to be consistent with other investigations
14	of MJO like oscillations, such as Hu and Randall (1994) and Raymond 2001. The
15	importance of <lw> is confirmed by a mechanism denial experiment. When the</lw>
16	radiative heating is homogenized zonally, the MJO-like disturbances disappear.
17	f) The latent heat flux anomalies associated with the MJO in our model are driven by
18	both surface moisture anomalies and wind speed anomalies, contrary to the typical
19	understanding of WISHE. Latent heat flux is also shown to be relatively
20	unimportant to both the maintenance and the propagation of the MJO-like
21	disturbance, in the sense of having only a small contribution to the MSE energy
22	budgets either in phase or in quadrature with the MSE anomaly. The relative

1	unimportance of LHF in our energy budget is in direct contradiction to many
2	studies that have observed LHF playing an important role in the MJO, such as
3	Maloney (2009) and Maloney et al. (2010).
4	g) The MSE sources associated with Eastward propagation of the anomaly are
5	dominated by to the combined actions of the horizontal and vertical advection of
6	MSE, which together create a positive MSE tendency ahead of the convective
7	center and a negative one over and behind it, retarded by the long-wave heating.
8	h) The MSE sources associated with poleward propagation are dominated by the
9	effect of horizontal advection of MSE, creating a positive tendency to polewards
10	and to the east of the convective center and a negative tendency to the west and
11	towards the equator. This advection is dominated by the meridional advection by
12	high frequency eddies – anomalous moistening ahead of the convection due to
13	suppression of eddy activity in this region – as observed by Maloney 2009. The
14	robustness of this result across several different modeling studies speaks of its
15	possible importance to the MJO on the Earth. Further, the good fit between our
16	parameterized eddy diffusion and the eddy meridional advection indicates the
17	validity of such a treatment.
18	i) The eddy advection, parameterized as diffusion, can be linearly approximated as
19	the sum of diffusion of the mean MSE by eddy anomalies and the diffusion of the
20	anomalous MSE by the mean eddies. The first quantity is seen to act as a source of
21	MSE associated with the eastward propagation, while the second dominates the
22	MSE sources associated with polewards propagation.

j) The eddy modulation is consistent with the modulation of barotropic conversion in
 the lower troposphere, due to the combined large-scale flow of the MJO and the
 mean state – suppressing conversion to the northeast and enhancing it to the north west.

k) The absence of an interactive ocean or an ENSO cycle in our model does not
preclude these mechanisms having an important role in the Earth's MJO. However,
the observation of the MJO in our fixed SST experiment does imply that SST
anomalies are not critical to the existence and propagation of MJO-like
disturbances.

10 Such is the nature of the current understanding of the MJO that the observations 11 reported here are consistent with (parts of) some studies and at odds with others. For 12 example, our results generally contradict those of Raymond (2001) regarding the 13 importance of latent heat flux while confirming the importance of cloud-radiation 14 feedback. Our results are also in agreement with Lin and Mapes (2004) regarding the 15 role of cloud-radiation feedback for the maintenance and propagation of the 16 disturbance; and Maloney (2009) on the importance of the meridional eddy advection 17 of MSE for the propagation of the anomaly. Investigation of the dependence of the 18 budget upon the mean state in the style of Maloney et al. (2010) is beyond the scope 19 of the current study, as we have limited our discussion to a single mean state. 20 However, the response of the observed mechanisms in SPCAM to variations in the 21 mean state is an avenue of research that we intend to pursue. Specifically, we will be 22 analyzing how the balance between the budget terms varies with ITCZ width.

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## 1 List of Figures

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3 Column Moisture, and d) 850hPa Zonal Wind. Error bars indicate the standard deviation 4 of the zonal mean of the time mean values. 5 FIG. 2. Logarithm (base 10) of the spectral power for signals symmetric about the 6 equator in a) OLR, and b) MSE for the control case and OLR for the c) MSE Damped 7 and d) LW Denial cases. The power spectrum is averaged over the region 15°S to 15°N 8 and is constructed from model output. (after Wheeler and Kiladis 1999). The 9 wavenumber zero data for panels c) and d) is deleted as it is rendered meaningless by the 10 experimental procedure. 11 FIG. 3. Hovmöller diagrams a) Unfiltered precipitation signal (averaged over  $0^{\circ}$ N- $6^{\circ}$ N); 12 b) MJO frequency-wavenumber filtered precipitation signal (averaged over  $0^{\circ}N-6^{\circ}N$ ); c) 13 Unfiltered precipitation signal (averaged over 160°E-160°W); 14 FIG. 4. Composite anomalies for the MJO like disturbances produced by regression, scaled to a -40W/m<sup>2</sup> OLR anomaly. a) Outgoing Longwave Radiation; b) Precipitation; 15 16 c) column integrated moisture. 17 FIG. 5. Composite winds anomalies for the MJO like disturbances produced by regression, scaled to a -40 W/m<sup>2</sup> OLR anomaly. a) 850hPa (maximum wind speed 5.1 18 19 m/s) and stream function; b) 200hPa (maximum wind speed 11.2 m/s) and stream 20 function; c) Vertical-meridional cross section of MJO regressed zonal wind at the 21 reference longitude.

FIG. 1. Time and zonal mean climate: a) Sea Surface Temperature, b) Precipitation, c)

1	FIG. 6. MJO regressed MSE and column MSE budget terms. a) Zonal-Vertical cross-
2	section along the ITCZ peak; b) Column integrated MSE anomaly; c) Column integrated
3	MSE time tendency; d) MJO regressed residual.
4	FIG. 7. a) Fractional contributions of the MSE budget terms to the
5	maintenance/dissipation of the MJO MSE anomaly. b) Fractional contributions of the
6	MSE budget terms to the propagation of the MJO MSE anomaly.
7	FIG. 8. Leading terms in the MJO regressed column MSE budget. a) Column integrated
8	long wave radiation forcing; b) Column integrated horizontal advection of MSE; c)
9	Column integrated vertical advection of MSE (equivalent to column integrated MSE
10	convergence); d) Total column integrated advection of MSE.
11	FIG. 9. Latent Heating Terms. a) MJO regressed Latent Heat Flux Anomaly; b) MJO
12	Latent Heating anomaly attributable to changes in surface level windspeed in a bulk
13	surface flux calculation; c) MJO Latent Heating anomaly attributable to changes in
14	surface level moisture content in a bulk surface flux calculation; d) Total bulk surface
15	scheme latent heat flux anomaly.
16	FIG. 10. a) Column integrated zonal advection of MSE; b) Column integrated meridional
17	advection of MSE; c) column integrated, MJO regressed, high frequency $v$ -high
18	frequency <i>h</i> advection.
19	FIG. 11. Eddy Diffusion of MSE anomalies. a) Diffusion of mean MSE by MJO eddy
20	anomalies; b) Diffusion of eddy MSE anomalies by mean eddy activity; c) Total eddy

21 diffusion of MSE. All figures are in arbitrary but consistent units.

- 2 Energy (EKE) anomaly at N; c) Anomalous Eddy Meridional Advection of MSE at N;
- 3 and d) Eddy Kinetic Energy (EKE) anomaly at N. MJO regression point is located at
- 4 Note the differences in vertical scale between the first and second pair of figures.
- 5 FIG. 13. a) The MJO regressed EKE anomaly at 850 hPa; b) EKE source due to
- 6 barotropic conversion of energy from the large scale winds at 850 hPa.



FIG. 1. Time and zonal mean climate: a) Sea Surface Temperature, b) Precipitation, c)
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- 2 FIG. 4. Composite anomalies for the MJO like disturbances produced by regression,
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- 4 c) column integrated moisture.



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FIG. 5. Composite winds anomalies (vectors) for the MJO like disturbances produced by regression and stream function (contours), scaled to a -40W/m<sup>2</sup> OLR anomaly. a) 850hPa 3 4 (maximum wind speed 5.1 m/s); b) 200hPa (maximum wind speed 11.2 m/s); c) Vertical-5 meridional cross section of MJO regressed zonal wind at the reference longitude.



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- 3 section along the ITCZ peak; b) Column integrated MSE anomaly; c) Column integrated
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- 4 maintenance/dissipation of the MJO MSE anomaly. b) Fractional contributions of the
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- 4 frequency *h* advection.




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FIG. 12. a) Anomalous Eddy Meridional Advection of MSE at N; b) Eddy Kinetic
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