Abstract Data Types 
and Data Structures

Unit 6, Part 1

Congrats on completing the first half!

• In the second half, we will study fundamental data structures.
  • ways of imposing order on a collection of information
  • sequences: lists, stacks, and queues
  • trees
  • hash tables
  • graphs

• We will also:
  • study algorithms related to these data structures
  • learn how to compare data structures & algorithms

• Goals:
  • learn to think more intelligently about programming problems
  • acquire a set of useful tools and techniques
Sample Problem I: Finding Shortest Paths

- Given a set of routes between pairs of cities, determine the shortest path from city A to city B.

![Graph of cities and routes with distances]

Sample Problem II: A Data "Dictionary"

- Given a large collection of data, how can we arrange it so that we can efficiently:
  - add a new item
  - search for an existing item

- Some data structures provide better performance than others for this application.

- More generally, we'll learn how to characterize the efficiency of different data structures and their associated algorithms.
Example of Comparing Algorithms

• Consider the problem of finding a phone number in a phonebook.

• Let’s informally compare the time efficiency of two algorithms for this problem.

<table>
<thead>
<tr>
<th>Algorithm 1 for Finding a Phone Number</th>
</tr>
</thead>
<tbody>
<tr>
<td>findNumber(person) {</td>
</tr>
<tr>
<td>for (p = number of first page; p &lt;= number of the last page; p++) {</td>
</tr>
<tr>
<td>if person is found on page p {</td>
</tr>
<tr>
<td>return the person’s phone number</td>
</tr>
<tr>
<td>}</td>
</tr>
<tr>
<td>}</td>
</tr>
<tr>
<td>return NOT_FOUND</td>
</tr>
<tr>
<td>}</td>
</tr>
</tbody>
</table>

• If there were 1,000 pages in the phonebook, how many pages would this look at in the worst case?
• What if there were 1,000,000 pages?
Algorithm 2 for Finding a Phone Number

```
findNumber(person) {
    min = the number of the first page
    max = the number of the last page
    while (min <= max) {
        mid = (min + max) / 2        // page number of the middle page
        if person is found on page mid {
            return the person's number
        } else if the person's name comes earlier in the book {
            max = mid – 1
        } else {
            min = mid + 1
        }
    }
    return NOT_FOUND
}
```

- If there were 1,000 pages in the phonebook, how many pages would this look at in the worst case?
- What if there were 1,000,000 pages?

Searching a Collection of Data

- The phonebook problem is one example of a common task: searching for an item in a collection of data.
  - another example: searching for a record in a database

- Algorithm 1 is known as _sequential search._
  - also called _linear search_

- Algorithm 2 is known as _binary search._
  - only works if the items in the data collection are sorted
Abstract Data Types

- An abstract data type (ADT) is a model of a data structure that specifies:
  - the characteristics of the collection of data
  - the operations that can be performed on the collection

- It’s abstract because it doesn’t specify how the ADT will be implemented.
  - does not commit to any low-level details

- A given ADT can have multiple implementations.

A Simple ADT: A Bag

- A bag is just a container for a group of data items.
  - analogy: a bag of candy

- The positions of the data items don’t matter (unlike a list).
  - \{3, 2, 10, 6\} is equivalent to \{2, 3, 6, 10\}

- The items do not need to be unique (unlike a set).
  - \{7, 2, 10, 7, 5\} isn’t a set, but it is a bag
A Simple ADT: A Bag (cont.)

- The operations we want a Bag to support:
  - `add(item)`: add item to the Bag
  - `remove(item)`: remove one occurrence of item (if any) from the Bag
  - `contains(item)`: check if item is in the Bag
  - `numItems()`: get the number of items in the Bag
  - `grab()`: get an item at random, without removing it
    - reflects the fact that the items don't have a position (and thus we can't say "get the 5th item in the Bag")
  - `toArray()`: get an array containing the current contents of the bag

- We want the bag to be able to store objects of any type.

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Specifying an ADT Using an Interface

- In Java, we can use an interface to specify an ADT:
  ```java
  public interface Bag {
    boolean add(Object item);
    boolean remove(Object item);
    boolean contains(Object item);
    int numItems();
    Object grab();
    Object[] toArray();
  }
  ```

- An interface specifies a set of methods.
  - includes only the method headers
  - does not typically include the full method definitions

- Like a class, it must go in a file with an appropriate name.
  - in this case: `Bag.java`
Implementing an ADT Using a Class

• To implement an ADT, we define a class:

```java
public class ArrayBag implements Bag {
    ...
    public boolean add(Object item) {
        ...
    }
}
```

• When a class header includes an implements clause, the class must define all of the methods in the interface.
  • if the class doesn't define them, it won't compile

All Interface Methods Are Public

• Methods specified in an interface must be public, so we don't use the keyword public in the definition:

```java
public interface Bag {
    boolean add(Object item);
    boolean remove(Object item);
    boolean contains(Object item);
    int numItems();
    Object grab();
    Object[] toArray();
}
```

• However, when we actually implement the methods in a class, we do need to use public:

```java
public class ArrayBag implements Bag {
    ...
    public boolean add(Object item) {
        ...
    }
}
```
One Possible Bag Implementation

• One way to store the items in the bag is to use an array:
  
  ```java
  public class ArrayBag {
      private ______________[] items;
      ...
  }
  ```

• What type should the array be?

• This allows us to store any type of object in the items array, thanks to the power of polymorphism:
  ```java
  ArrayBag bag = new ArrayBag();
  bag.add("hello");
  bag.add(new Rectangle(20, 30));
  ```

• How could we keep track of how many items are in a bag?

Another Example of Polymorphism

• An interface name can be used as the type of a variable:
  ```java
  Bag b;
  ```

• Variables with an interface type can refer to objects of any class that implements the interface:
  ```java
  Bag b = new ArrayBag();
  ```

• Using the interface as the type allows us to write code that works with any implementation of an ADT:
  ```java
  public void processBag(Bag b) {
      for (int i = 0; i < b.numItems(); i++) {
          ...
      }
  }
  ```

• the param can be an instance of any Bag implementation
• we must use method calls to access the object's internals, because the fields are not part of the interface
Memory Management: Looking Under the Hood

- To understand how data structures are implemented, you need to understand how memory is managed.

- There are three main types of memory allocation in Java.

- They correspond to three different regions of memory.

Memory Management, Type I: Static Storage

- Static storage is used for class variables, which are declared outside any method using the keyword static:

```java
public class MyMethods {
    public static int numCompares;
    public static final double PI = 3.14159;
}
```

- There is only one copy of each class variable.
  - shared by all objects of the class
  - Java's version of a global variable

- The Java runtime allocates memory for class variables when the class is first encountered.
  - this memory stays fixed for the duration of the program
Memory Management, Type II: Stack Storage

• Method parameters and local variables are stored in a region of memory known as the stack.

• For each method call, a new stack frame is added to the top of the stack.

```java
public class Foo {
    public static int x(int i) {
        int j = i - 2;
        if (i >= 6) {
            return i;
        } else {
            return x(i + j);
        }
    }
    public static void main(String[] args) {
        System.out.println(x(5));
    }
}
```

• When a method completes, its stack frame is removed.

Memory Management, Type III: Heap Storage

• Objects are stored in a memory region known as the heap.

• Memory on the heap is allocated using the new operator:

```java
int[] values = new int[3];
ArrayBag b = new ArrayBag();
```

• new returns the memory address of the start of the object on the heap.
  • a reference!

• An object stays on the heap until there are no remaining references to it.

• Unused objects are automatically reclaimed by a process known as garbage collection.
  • makes their memory available for other objects
Two Constructors for the ArrayBag Class

public class ArrayBag implements Bag {
    private Object[] items;
    private int numItems;
    public static final int DEFAULT_MAX_SIZE = 50;

    public ArrayBag() {
        this.items = new Object[DEFAULT_MAX_SIZE];
        this.numItems = 0;
    }

    public ArrayBag(int maxSize) {
        if (maxSize <= 0) {
            throw new IllegalArgumentException(
                    "maxSize must be > 0");
        } else {
            this.items = new Object[maxSize];
            this.numItems = 0;
        }
    }

    ...
}

- As we've seen before, we can have multiple constructors.
  - the parameters must differ in some way
- The first one is useful for small bags.
  - creates an array with room for 50 items.
- The second one allows the client to specify the max # of items.

- If the user inputs an invalid maxSize, we throw an exception.
Example: Creating Two ArrayBag Objects

```java
// client
public static void main(String[] args) {
    ArrayBag b1 = new ArrayBag(2);
    ArrayBag b2 = new ArrayBag(4);
    ...
}
```

```java
// constructor
public ArrayBag(int maxSize) {
    ... // error-checking
    this.items = new Object[maxSize];
    this.numItems = 0;
}
```

After the objects have been created, here's what we have:

- `b1` and `b2` are two ArrayBag objects.
- `args` is an array of strings.
- `items` and `numItems` are null.
- `maxSize` is set to 2 for `b1` and 4 for `b2`.

The diagram shows the stack and heap memory allocations for the objects and their associated variables.
Adding Items

- We fill the array from left to right. Here's an empty bag:

```
items  numItems
0      null null null null
```

- After adding the first item:

```
items  numItems
1      null null null null
     "hello, world"
```

- After adding the second item:

```
items  numItems
2      null null null
     "hello, world" "howdy"
```

Adding Items (cont.)

- After adding the third item:

```
items  numItems
3      null null
     "hello, world" "howdy" "bye"
```

- After adding the fourth item:

```
items  numItems
4      null
     "hello, world" "howdy" "bye" "see ya!"
```

- At this point, the ArrayBag is full!
  - it's non-trivial to "grow" an array, so we don't!
  - additional items cannot be added until one is removed
A Method for Adding an Item to a Bag

public class ArrayBag implements Bag {
    private Object[] items;
    private int numItems;
    ...
    public boolean add(Object item) {
        if (item == null) {
            throw new IllegalArgumentException("no nulls");
        } else if (this.numItems == this.items.length) {
            return false; // no more room!
        } else {
            this.items[this.numItems] = item;
            this.numItems++;
            return true;  // success!
        }
    }
}

- takes an object of any type!
- returns a boolean to indicate if the operation succeeded

Initially, this.numItems is 0, so the first item goes in position 0.
We increase this.numItems because we now have 1 more item.
- and so the next item added will go in the correct position!
Example: Adding an Item

```java
class ArrayBag {
    private Object[] items;
    private int numItems;

    public boolean add(Object item) {
        if (this.numItems < items.length - 1) {
            this.items[this.numItems] = item;
            this.numItems++;
            return true;
        } else {
            return false;
        }
    }
}
```

Example: Adding an Item (cont.)

```java
class ArrayBag {
    private Object[] items;
    private int numItems;

    public boolean add(Object item) {
        if (this.numItems < items.length - 1) {
            this.items[this.numItems] = item;
            this.numItems++;
            return true;
        } else {
            return false;
        }
    }
}
```

- add's stack frame includes:
  - item, which stores...
  - this, which stores...
The method modifies the items array and numItems.
- note that the array holds a copy of the reference to the item, not a copy of the item itself.

After the method call returns, add's stack frame is removed from the stack.
Extra Practice: Determining if a Bag Contains an Item

Let’s write the ArrayBag contains() method together.

- should return true if an object equal to item is found,
  and false otherwise.

```java
_________________ contains(_____________ item) {
}
```
Would this work instead?

- Let's write the ArrayBag `contains()` method together.
  - should return `true` if an object equal to `item` is found, and `false` otherwise.

```java
public boolean contains(Object item) {
    for (int i = 0; i < this.items.length; i++) {
        if (this.items[i].equals(item)) { // not ==
            return true;
        }
    }
    return false;
}
```

Another Incorrect `contains()` Method

```java
public boolean contains(Object item) {
    for (int i = 0; i < this.numItems; i++) {
        if (this.items[i].equals(item)) { // not ==
            return true;
        } else {
            return false;
        }
    }
    return false;
}
```

- What's the problem with this?
A Method That Takes a Bag as a Parameter

```java
public boolean containsAll(Bag otherBag) {
    if (otherBag == null || otherBag.numItems() == 0) {
        return false;
    }
    Object[] otherItems = otherBag.toArray();
    for (int i = 0; i < otherItems.length; i++) {
        if (!this.contains(otherItems[i])) {
            return false;
        }
    }
    return true;
}
```

- We use `Bag` instead of `ArrayBag` as the type of the parameter.
  - allows this method to be part of the `Bag` interface
  - allows us to pass in any object that implements `Bag`
- We must use methods in the interface to manipulate `otherBag`.
  - we can't use the fields, because they're not in the interface

A Type Mismatch

- Here are the headers of two `ArrayBag` methods:
  ```java
  public boolean add(Object item)
  public Object grab()
  ```
- Polymorphism allows us to pass `String` objects into `add()`:
  ```java
  ArrayBag stringBag = new ArrayBag();
  stringBag.add("hello");
  stringBag.add("world");
  ```
- However, this will not work:
  ```java
  String str = stringBag.grab();   // compiler error
  ```
  - the return type of `grab()` is `Object`
  - `Object` isn't a subclass of `String`, so polymorphism doesn't help!
- Instead, we need to use a type cast:
  ```java
  String str = (String)stringBag.grab();
  ```
  - this cast doesn't actually change the value being assigned
  - it just reassures the compiler that the assignment is okay